

Max Volume?

$$\begin{aligned}
 V(x) &= x(10 - 2x)\left(\frac{15 - 2x}{2}\right) \\
 &= (10x - 2x^2)\left(\frac{15 - 2x}{2}\right) \\
 &= (10x - 2x^2)(\frac{15}{2} - x) \\
 &= 10x\left(\frac{15}{2}\right) - 10x^2 - 2x^2\left(\frac{15}{2}\right) + 2x^3 \\
 &= 75x - 10x^2 - 15x^2 + 2x^3 \\
 V(x) &= 2x^3 - 25x^2 + 75x
 \end{aligned}$$

b) Domain  $x$ -values that make sense

$$\begin{aligned}
 w &= 10 - 2x & \Rightarrow & 0 < x < 5 \\
 h &= x & \Rightarrow & \\
 l &= \frac{15 - 2x}{2} & \Rightarrow & 
 \end{aligned}$$

c) Use Desmos look at the graph between  $0 < x < 5$ 

$$\begin{aligned}
 V(x) & \\
 \text{Volume} &\approx 66 \text{ in}^3 \\
 x &\approx 1.96 \text{ in}
 \end{aligned}$$

d)  $V(x) = 2x^3 - 25x^2 + 75x$

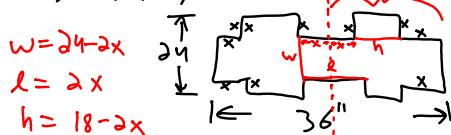
$$\begin{aligned}
 V'(x) &= 6x^2 - 50x + 75 \\
 x &= 1.96
 \end{aligned}$$

From (b) the domain  $\Rightarrow 0 < x < 5$

$$\therefore x \neq 1.96$$

$$\begin{aligned}
 x &= 1.96 \\
 V(1.96) &= 2(1.96)^3 - 25(1.96)^2 + 75(1.96)
 \end{aligned}$$

$$V(1.96) = 66.02 \text{ in}^3$$

19)  $V(x)$  want max volume

Finish #19 for HW 12/3/13